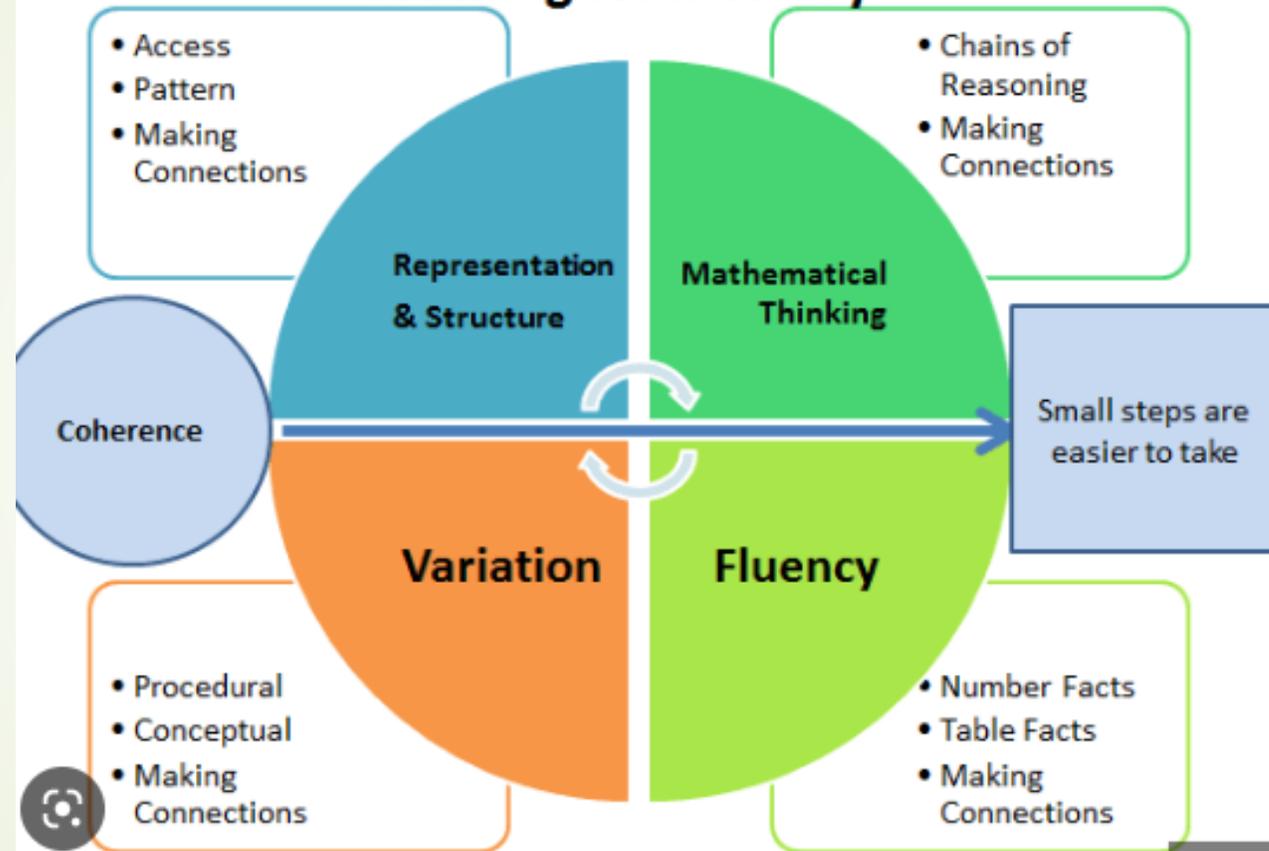




Maths Parents workshop

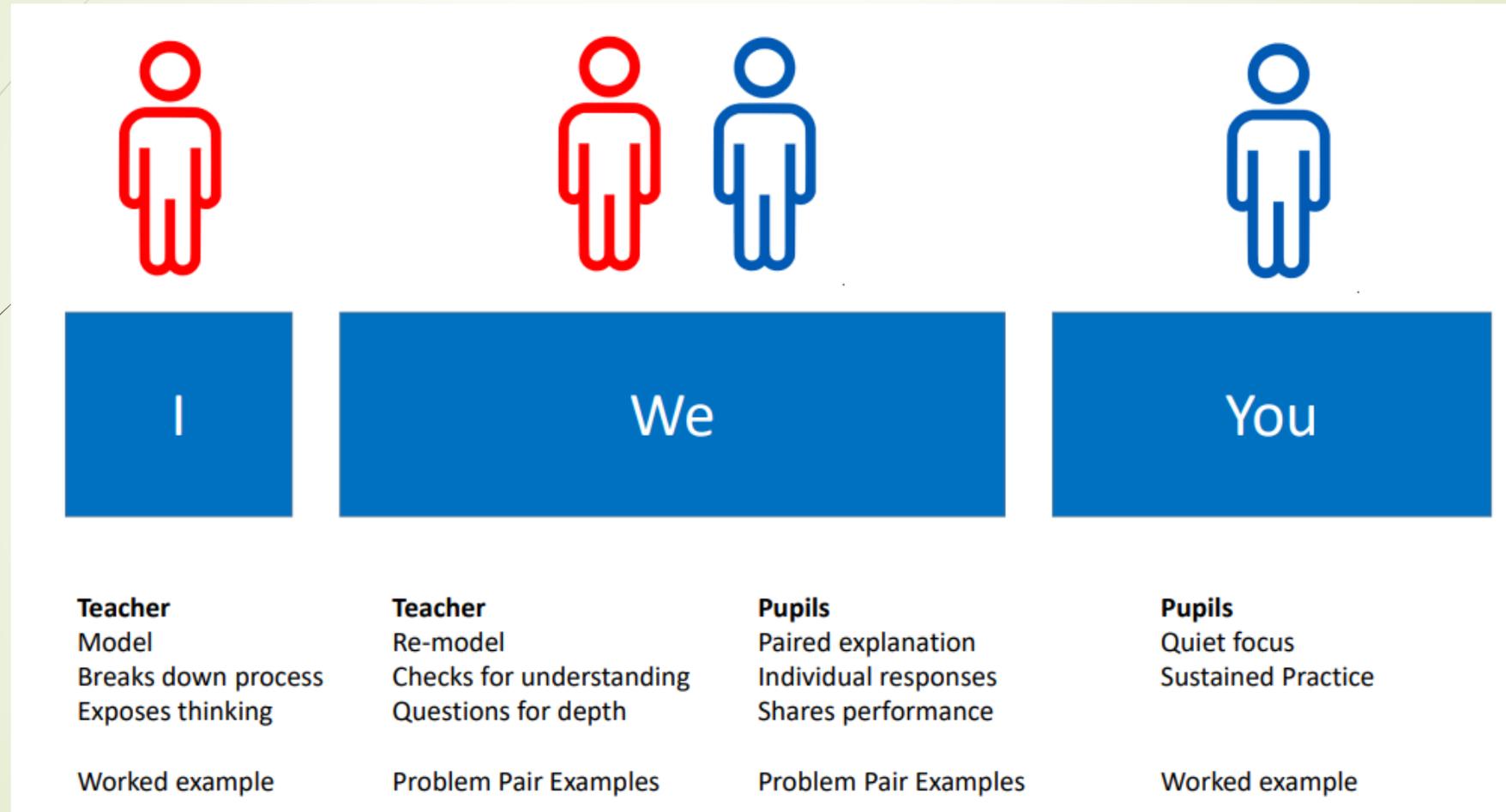
29th November

Teaching for Mastery



How it looks in action.

- Teacher teach whole class input, TA supports





Stem sentences and generalisations

Rationale for using stems and generalisations.

Maintaining children's **focus**...

Enabling all children to recognise **what's important** and what needs to be **remembered** for later learning.

Reducing cognitive load to enable learning to happen.

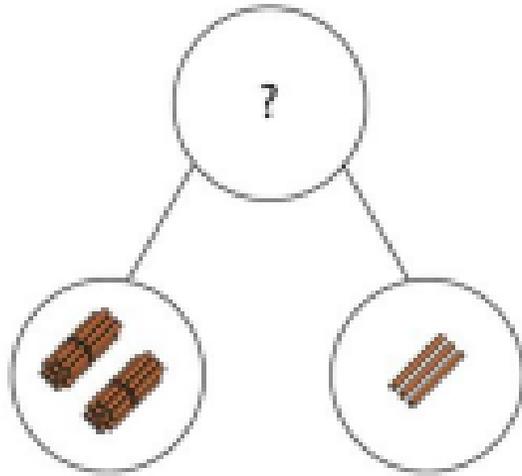
Returning to ideas and enabling ideas to be **connected**.

Providing the **correct language** for all children to **think** about and **communicate** mathematical ideas.

Providing high quality **shared** language to **discuss**, connect and share ideas.

Try this stem

There are ___ tens which is ___ and ___ ones which is ____.
This makes ___ altogether.



There are two tens which is twenty and three ones which is three. This makes twenty-three altogether: 23.

The '2' represents two tens. It has a value of twenty.

The '3' represents three ones. It has a value of three.



Generalisations:

*'Understanding the underlying structures of mathematics is **fundamental to mastering** the subject. This involves being fluent at **generalising and proving.**'*

Pennant and Woodham (2018)

Make 37

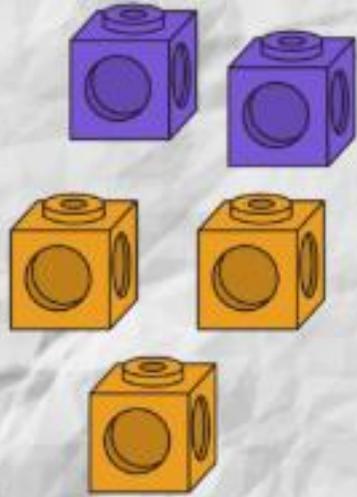


Four bags contain a large number of 1s, 3s, 5s and 7s.

Can you pick ten numbers from the bags that add up to 37?



Concrete



Pictorial



Abstract

$$3 + 2 = 5$$



MathShed



Addition

EYFS and KS1

Knowing and finding number bonds within 10

Break apart a group and put back together to find and form number bonds.

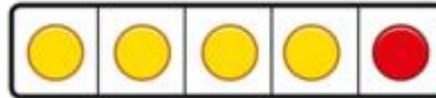


$$3 + 4 = 7$$

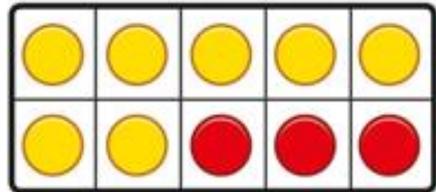


$$6 = 2 + 4$$

Use five and ten frames to represent key number bonds.

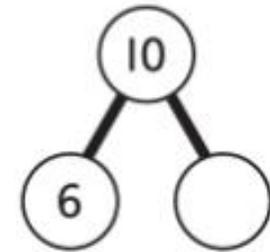
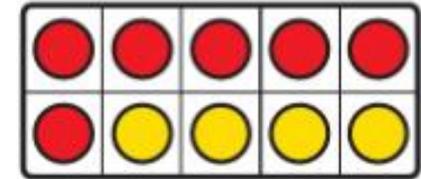


$$5 = 4 + 1$$



$$10 = 7 + 3$$

Use a part-whole model alongside other representations to find number bonds.

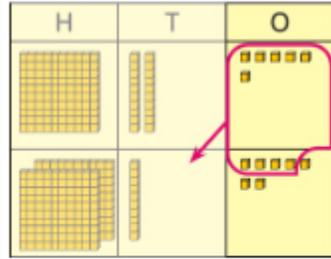


Make sure to include examples where one of the parts is zero.

LKS2

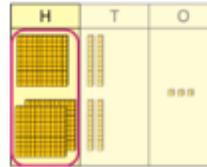
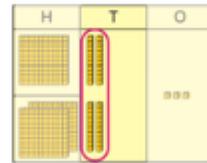
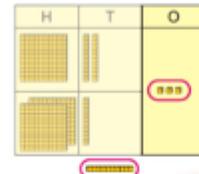
**3-digit number
+ 3-digit
number,
exchange
required**

Use place value equipment to enact the exchange required.



*There are 13 ones.
I will exchange 10 ones for 1 ten.*

Model the stages of column addition using place value equipment on a place value grid.



Use column addition, ensuring understanding of place value at every stage of the calculation.

	H	T	O
	1	2	6
+	2	1	7
			3

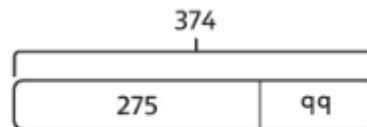
	H	T	O
	1	2	6
+	2	1	7
		4	3
			1

	H	T	O
	1	2	6
+	2	1	7
	3	4	3
			1

$$126 + 217 = 343$$

Children understand and create bar models to represent addition problems.

$$275 + 99 = ?$$



$$275 + 99 = 374$$

UPKS2

	Concrete	Pictorial	Abstract																																																																																																										
Year 6 Addition																																																																																																													
Comparing and selecting efficient methods	<p>Represent 7-digit numbers on a place value grid and use this to support thinking and mental methods.</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th>M</th> <th>HTh</th> <th>TTh</th> <th>Th</th> <th>H</th> <th>T</th> <th>O</th> </tr> </thead> <tbody> <tr> <td>••</td> <td>••••</td> <td>•</td> <td>•</td> <td>•••</td> <td></td> <td>•</td> </tr> </tbody> </table>	M	HTh	TTh	Th	H	T	O	••	••••	•	•	•••		•	<p>Discuss similarities and differences between methods, and choose efficient methods based on the specific calculation. Compare written and mental methods alongside place value representations.</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;"> <p>?</p> <table border="1"> <tr> <td>40,365</td> <td>3,572</td> </tr> </table> </div> <table border="1" style="border-collapse: collapse;"> <thead> <tr> <th></th> <th>TTh</th> <th>Th</th> <th>H</th> <th>T</th> <th>O</th> </tr> </thead> <tbody> <tr> <td></td> <td>4</td> <td>0</td> <td>3</td> <td>6</td> <td>5</td> </tr> <tr> <td>+</td> <td></td> <td>3</td> <td>5</td> <td>7</td> <td>2</td> </tr> <tr> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> </tr> <tr> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> </tr> </tbody> </table> </div> <p>Use bar model and number line representations to model addition in problem-solving and measure contexts.</p> <div style="text-align: center;"> </div>	40,365	3,572		TTh	Th	H	T	O		4	0	3	6	5	+		3	5	7	2													<p>Use column addition where mental methods are not efficient. Recognise common errors with column addition.</p> <p>$32,145 + 4,302 = ?$</p> <div style="display: flex; justify-content: space-around; align-items: flex-start;"> <table border="1" style="border-collapse: collapse;"> <thead> <tr> <th>TTh</th> <th>Th</th> <th>H</th> <th>T</th> <th>O</th> </tr> </thead> <tbody> <tr> <td>3</td> <td>2</td> <td>1</td> <td>4</td> <td>5</td> </tr> <tr> <td>+</td> <td>4</td> <td>3</td> <td>0</td> <td>2</td> </tr> <tr> <td></td> <td>3</td> <td>6</td> <td>4</td> <td>7</td> </tr> </tbody> </table> <table border="1" style="border-collapse: collapse;"> <thead> <tr> <th>TTh</th> <th>Th</th> <th>H</th> <th>T</th> <th>O</th> </tr> </thead> <tbody> <tr> <td>3</td> <td>2</td> <td>1</td> <td>4</td> <td>5</td> </tr> <tr> <td>+</td> <td>4</td> <td>3</td> <td>0</td> <td>2</td> </tr> <tr> <td></td> <td>7</td> <td>5</td> <td>1</td> <td>6</td> </tr> </tbody> </table> </div> <p><i>Which method has been completed accurately?</i></p> <p><i>What mistake has been made?</i></p> <p>Column methods are also used for decimal additions where mental methods are not efficient.</p> <table border="1" style="border-collapse: collapse; margin-left: auto; margin-right: auto;"> <thead> <tr> <th>H</th> <th>T</th> <th>O</th> <th>Tth</th> <th>Hth</th> </tr> </thead> <tbody> <tr> <td>1</td> <td>4</td> <td>0</td> <td>0</td> <td>9</td> </tr> <tr> <td>+</td> <td>4</td> <td>9</td> <td>8</td> <td>9</td> </tr> <tr> <td></td> <td>1</td> <td>8</td> <td>9</td> <td>8</td> </tr> </tbody> </table>	TTh	Th	H	T	O	3	2	1	4	5	+	4	3	0	2		3	6	4	7	TTh	Th	H	T	O	3	2	1	4	5	+	4	3	0	2		7	5	1	6	H	T	O	Tth	Hth	1	4	0	0	9	+	4	9	8	9		1	8	9	8
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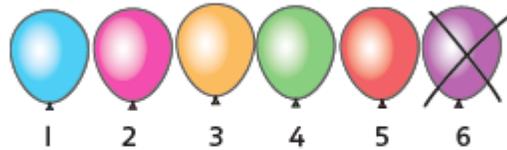


Subtraction

EYFS and KS1

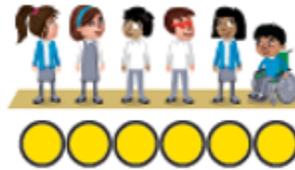
Counting back and taking away

Children arrange objects and remove to find how many are left.



1 less than 6 is 5.
6 subtract 1 is 5.

Children draw and cross out or use counters to represent objects from a problem.



Now there are 6 children.

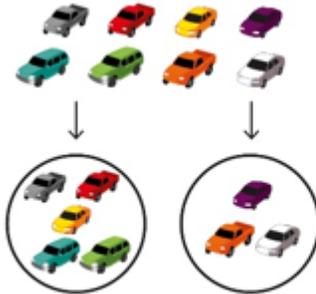
Children count back to take away and use a number line or number track to support the method.



$$9 - 3 = 6$$

Finding a missing part, given a whole and a part

Children separate a whole into parts and understand how one part can be found by subtraction.

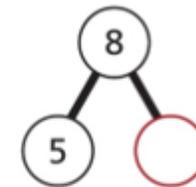


$$8 - 5 = ?$$

Children represent a whole and a part and understand how to find the missing part by subtraction.



Children use a part-whole model to support the subtraction to find a missing part.



$$8 - 5 = ?$$

Children develop an understanding of the relationship between addition and subtraction facts in a part-whole model.

Finding the difference

Arrange two groups so that the difference between the groups can be worked out.

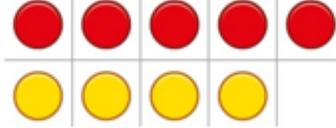


8 is 2 more than 6.

6 is 2 less than 8.

The difference between 8 and 6 is 2.

Represent objects using sketches or counters to support finding the difference.



$$5 - 4 = 1$$

The difference between 5 and 4 is 1.

Children understand 'find the difference' as subtraction.



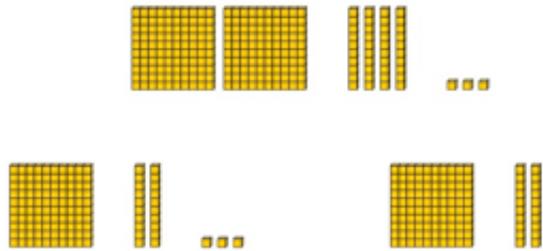
$$10 - 4 = 6$$

The difference between 10 and 6 is 4.

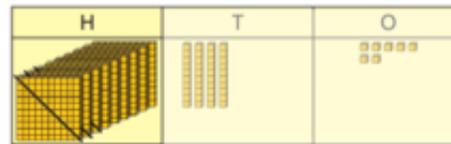
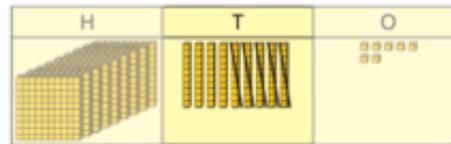
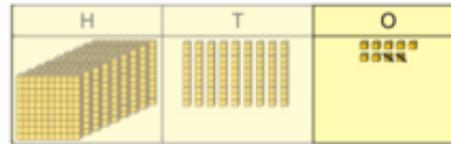
LKS2

3-digit number – up to 3-digit number

Use place value equipment to explore the effect of splitting a whole into two parts, and understand the link with taking away.



Represent the calculation on a place value grid.



Use column subtraction to calculate accurately and efficiently.

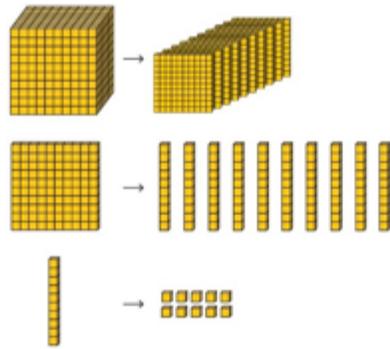
	H	T	O
	9	9	9
-	3	5	2
			7

	H	T	O
	9	9	9
-	3	5	2
		4	7

	H	T	O
	9	9	9
-	3	5	2
	6	4	7

Column subtraction

Understand why exchange of a 1,000 for 100s, a 100 for 10s, or a 10 for 1s may be necessary.



Represent place value equipment on a place value grid to subtract, including exchanges where needed.

Th	H	T	O
●	●●	●●●●●	

Th	H	T	O
●	●●	●●● ●●	

Th	H	T	O
●	●●●●● ●●	●●● ●●	

Th	H	T	O
	●●●●● ●●	●●● ●●	

Use column subtraction, with understanding of the place value of any exchange required.

	Th	H	T	O
	1	2	5	0
-		3	2	0
			3	0

	Th	H	T	O
	1	2	5	0
-		3	2	0
		9	3	0

	Th	H	T	O
	1	2	5	0
-		3	2	0
		9	3	0

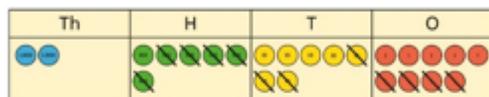
	Th	H	T	O
	1	2	5	0
-		3	2	0
		9	3	0

UKS2

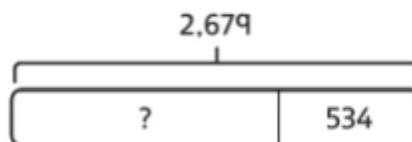
Year 6 Subtraction

Comparing and selecting efficient methods

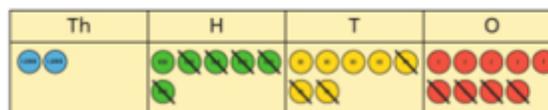
Use counters on a place value grid to represent subtractions of larger numbers.



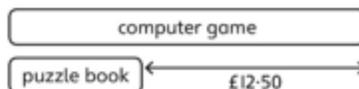
Compare subtraction methods alongside place value representations.



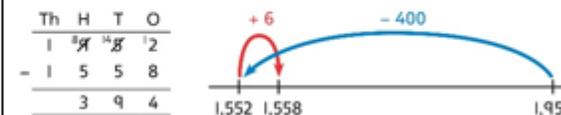
	Th	H	T	O
	2	6	7	9
-		5	3	4
	2	1	4	5



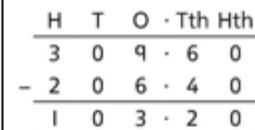
Use a bar model to represent calculations, including 'find the difference' with two bars as comparison.



Compare and select methods. Use column subtraction when mental methods are not efficient. Use two different methods for one calculation as a checking strategy.



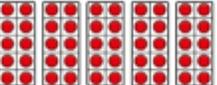
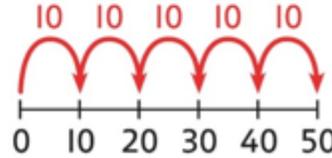
Use column subtraction for decimal problems, including in the context of measure.





Multiplication

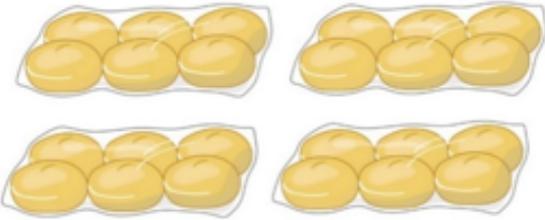
EYFS and KS1

<p>Recognising and making equal groups</p>	<p>Children arrange objects in equal and unequal groups and understand how to recognise whether they are equal.</p> <p>A  B  C </p>	<p>Children draw and represent equal and unequal groups.</p> <p>A  B </p>	<p><i>Three equal groups of 4. Four equal groups of 3.</i></p>																																																		
<p>Finding the total of equal groups by counting in 2s, 5s and 10s</p>	<p></p> <p>There are 5 pens in each pack ... 5... 10... 15... 20... 25... 30... 35... 40...</p>	<p>100 squares and ten frames support counting in 2s, 5s and 10s.</p> <p></p> <table border="1" data-bbox="1184 871 1439 1006"> <tbody> <tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr> <tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr> <tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr> <tr><td>31</td><td>32</td><td>33</td><td>34</td><td>35</td><td>36</td><td>37</td><td>38</td><td>39</td><td>40</td></tr> <tr><td>41</td><td>42</td><td>43</td><td>44</td><td>45</td><td>46</td><td>47</td><td>48</td><td>49</td><td>50</td></tr> </tbody> </table>	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	<p>Use a number line to support repeated addition through counting in 2s, 5s and 10s.</p> <p></p>
1	2	3	4	5	6	7	8	9	10																																												
11	12	13	14	15	16	17	18	19	20																																												
21	22	23	24	25	26	27	28	29	30																																												
31	32	33	34	35	36	37	38	39	40																																												
41	42	43	44	45	46	47	48	49	50																																												

LKS2

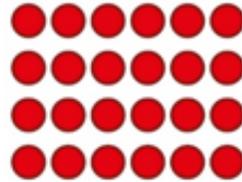
Using commutativity to support understanding of the times-tables

Understand how to use times-tables facts flexibly.



*There are 6 groups of 4 pens.
There are 4 groups of 6 bread rolls.
I can use $6 \times 4 = 24$ to work out both totals.*

Understand how times-table facts relate to commutativity.



$$6 \times 4 = 24$$
$$4 \times 6 = 24$$

Understand how times-table facts relate to commutativity.

I need to work out 4 groups of 7.

I know that $7 \times 4 = 28$

so, I know that

4 groups of 7 = 28

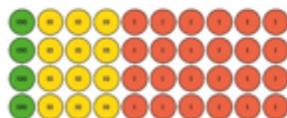
and

7 groups of 4 = 28.

Column multiplication for 2- and 3-digit numbers multiplied by a single digit

Use place value equipment to make multiplications.

Make 4×136 using equipment.

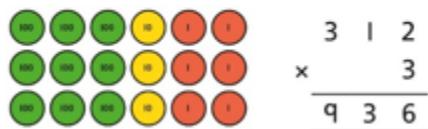


I can work out how many 1s, 10s and 100s.

There are 4×6 ones... 24 ones
 There are 4×3 tens ... 12 tens
 There are 4×1 hundreds ... 4 hundreds

$$24 + 120 + 400 = 544$$

Use place value equipment alongside a column method for multiplication of up to 3-digit numbers by a single digit.



Use the formal column method for up to 3-digit numbers multiplied by a single digit.

$$\begin{array}{r} 312 \\ \times \quad 3 \\ \hline 936 \end{array}$$

Understand how the expanded column method is related to the formal column method and understand how any exchanges are related to place value at each stage of the calculation.

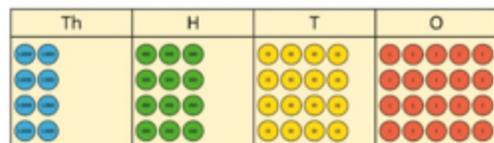
$$\begin{array}{r} 23 \\ \times \quad 5 \\ \hline 115 \end{array} \qquad \begin{array}{r} 23 \\ \times \quad 5 \\ \hline 115 \\ \hline \end{array}$$

UKS2

Year 6 Multiplication

Multiplying up to a 4-digit number by a single digit number

Use equipment to explore multiplications.



4 groups of 2,345

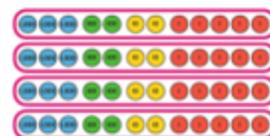
This is a multiplication:

$$4 \times 2,345$$

$$2,345 \times 4$$

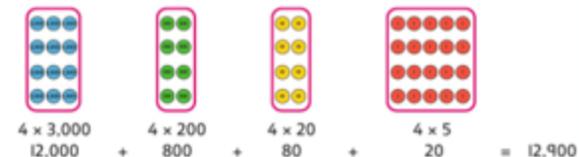
Use place value equipment to compare methods.

Method 1



		3	2	5	5
		3	2	2	5
		3	2	2	5
+		3	2	2	5
	1	2	9	0	0
	1				

Method 2



$$4 \times 3,000 = 12,000$$

$$4 \times 200 = 800$$

$$4 \times 20 = 80$$

$$4 \times 5 = 20$$

$$12,000 + 800 + 80 + 20 = 12,900$$

Understand area model and short multiplication.

Compare and select appropriate methods for specific multiplications.

Method 3

	3,000	200	20	5
4	12,000	800	80	20

$$12,000 + 800 + 80 + 20 = 12,900$$

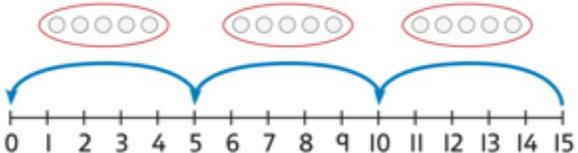
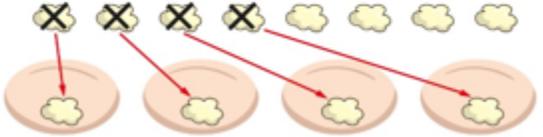
Method 4

		3	2	2	5
x					4
	1	2	9	0	0
	1				



Division

EYFS and KS1

Year 1 Division			
<p>Grouping</p> <p>Learn to make equal groups from a whole and find how many equal groups of a certain size can be made.</p> <p>Sort a whole set people and objects into equal groups.</p>  <p><i>There are 10 children altogether. There are 2 in each group. There are 5 groups.</i></p>	<p>Represent a whole and work out how many equal groups.</p>  <p><i>There are 10 in total. There are 5 in each group. There are 2 groups.</i></p>	<p>Children may relate this to counting back in steps of 2, 5 or 10.</p> 	
<p>Sharing</p> <p>Share a set of objects into equal parts and work out how many are in each part.</p> 	<p>Sketch or draw to represent sharing into equal parts. This may be related to fractions.</p> 	<p><i>10 shared into 2 equal groups gives 5 in each group.</i></p>	

LKS2

2-digit number divided by 1-digit number, with remainders

Use place value equipment to understand the concept of remainder.

Make 29 from place value equipment. Share it into 2 equal groups.



There are two groups of 14 and 1 remainder.

Use place value equipment to understand the concept of remainder in division.

$$29 \div 2 = ?$$



$$29 \div 2 = 14 \text{ remainder } 1$$

Partition to divide, understanding the remainder in context.

67 children try to make 5 equal lines.

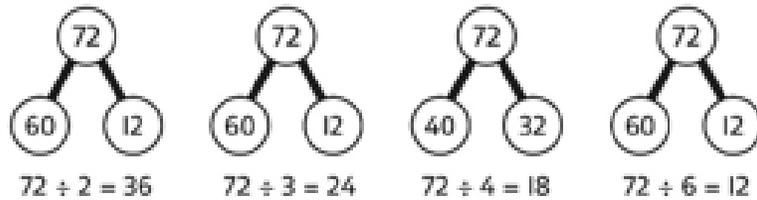
$$67 = 50 + 17$$
$$50 \div 5 = 10$$

$$17 \div 5 = 3 \text{ remainder } 2$$
$$67 \div 5 = 13 \text{ remainder } 2$$

There are 13 children in each line and 2 children left out.



Make decisions about appropriate partitioning based on the division required.



Understand that different partitions can be used to complete the same division.